Decreasing Complexity by Increasing Numbers

Part 1: The Law of Large Numbers

Christoph Becker

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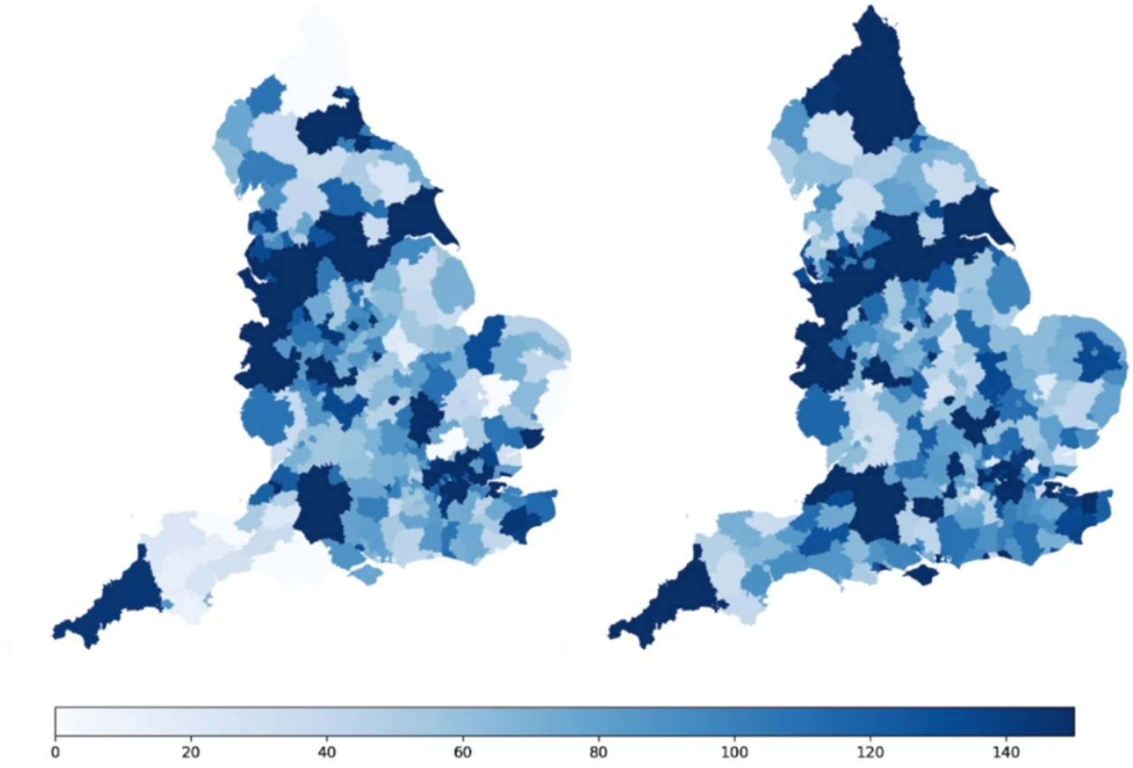
Who am I

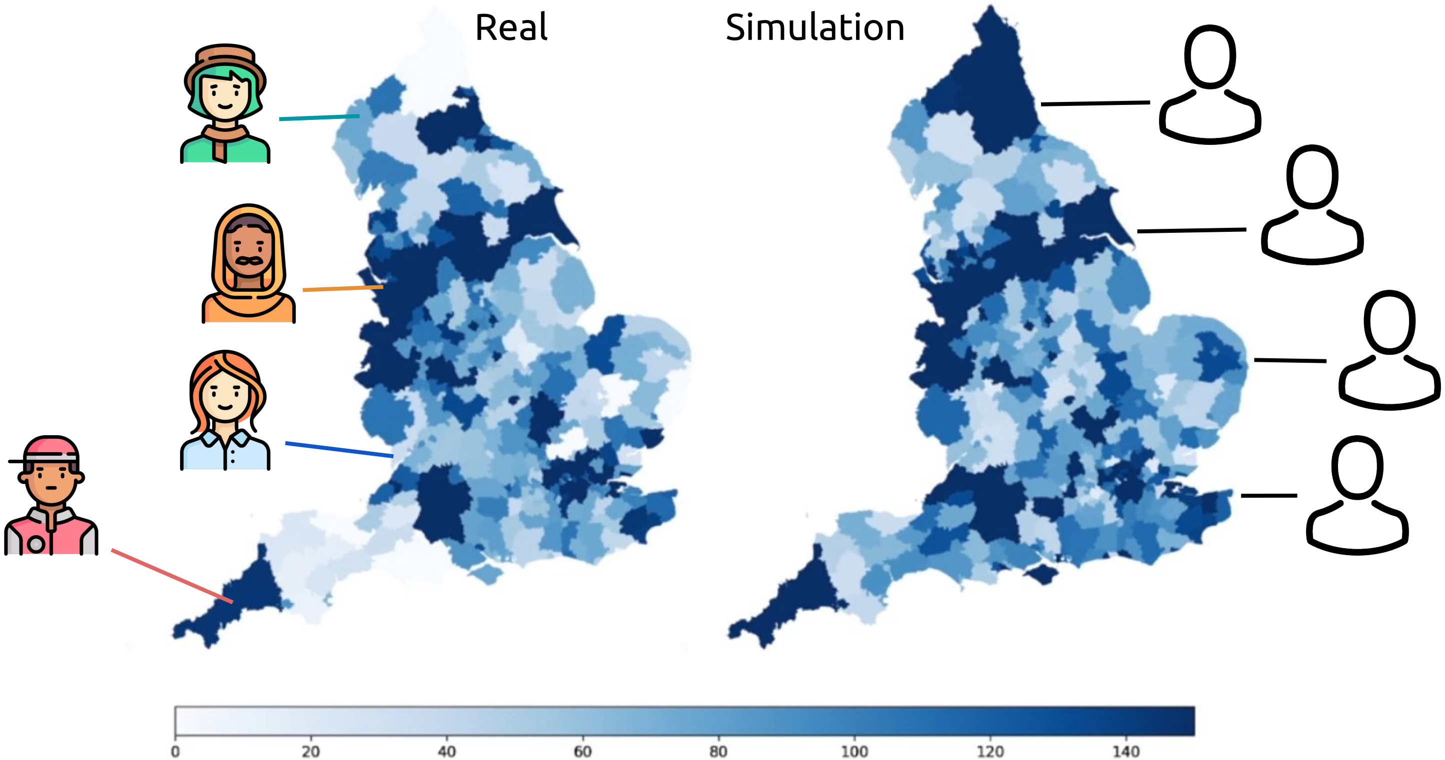
… Give a little introduction about yourself ...

The Covid-19 Pandemic in England



Covid-19 deaths from March to October

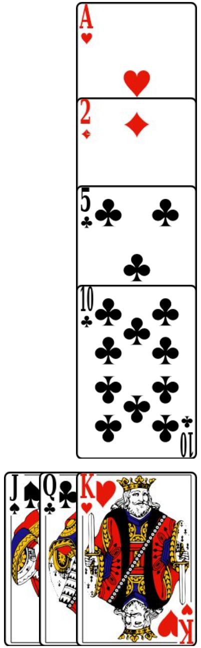
The Covid-19 Pandemic in England



Covid-19 deaths from March to October

The Law of Large Numbers — Kruskal Count

Card Value



1

2

...

5

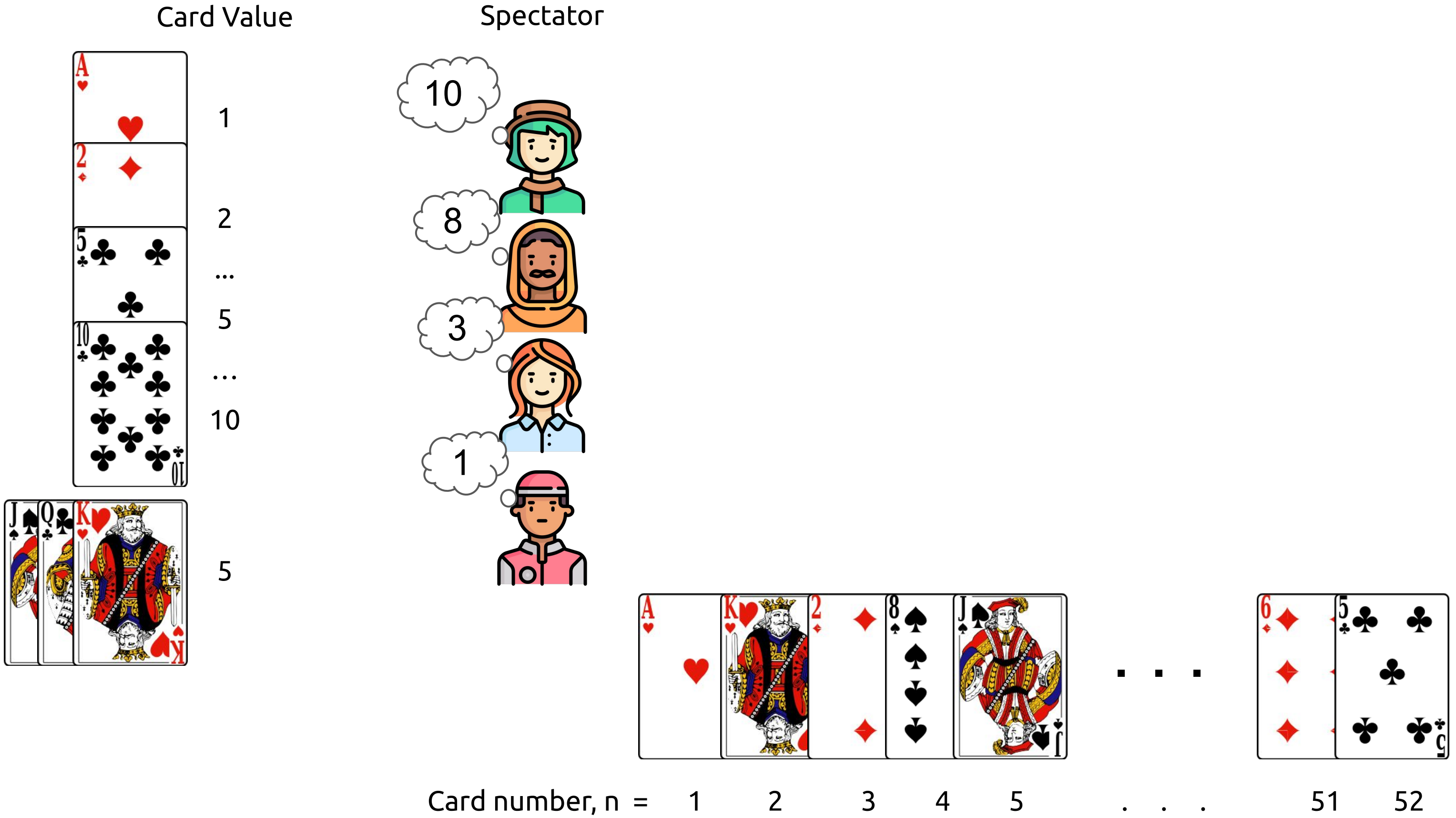
...

10

5

Card number, n = 1 2 3 4 5 . . . 51 52

The Law of Large Numbers — Kruskal Count



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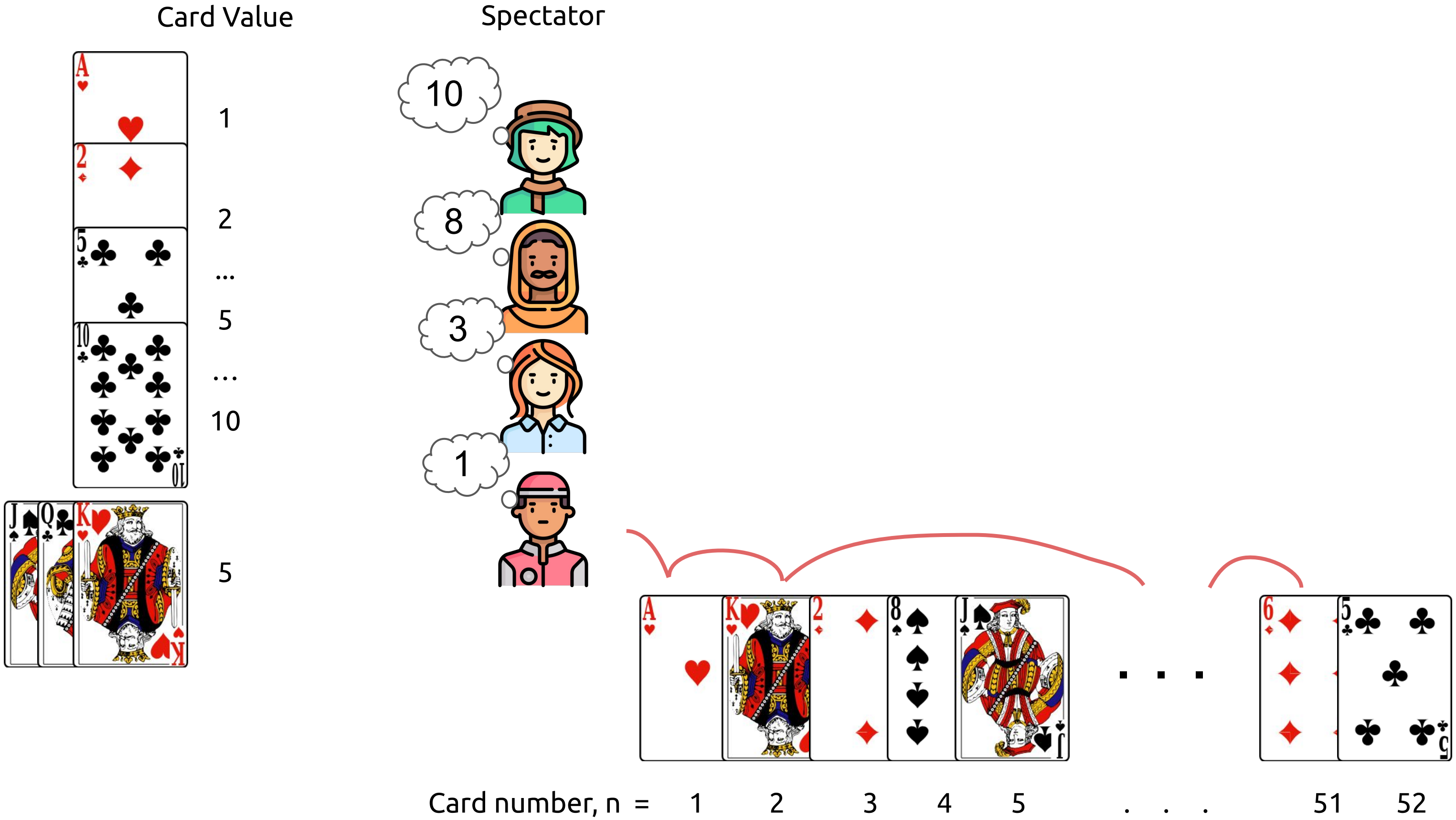
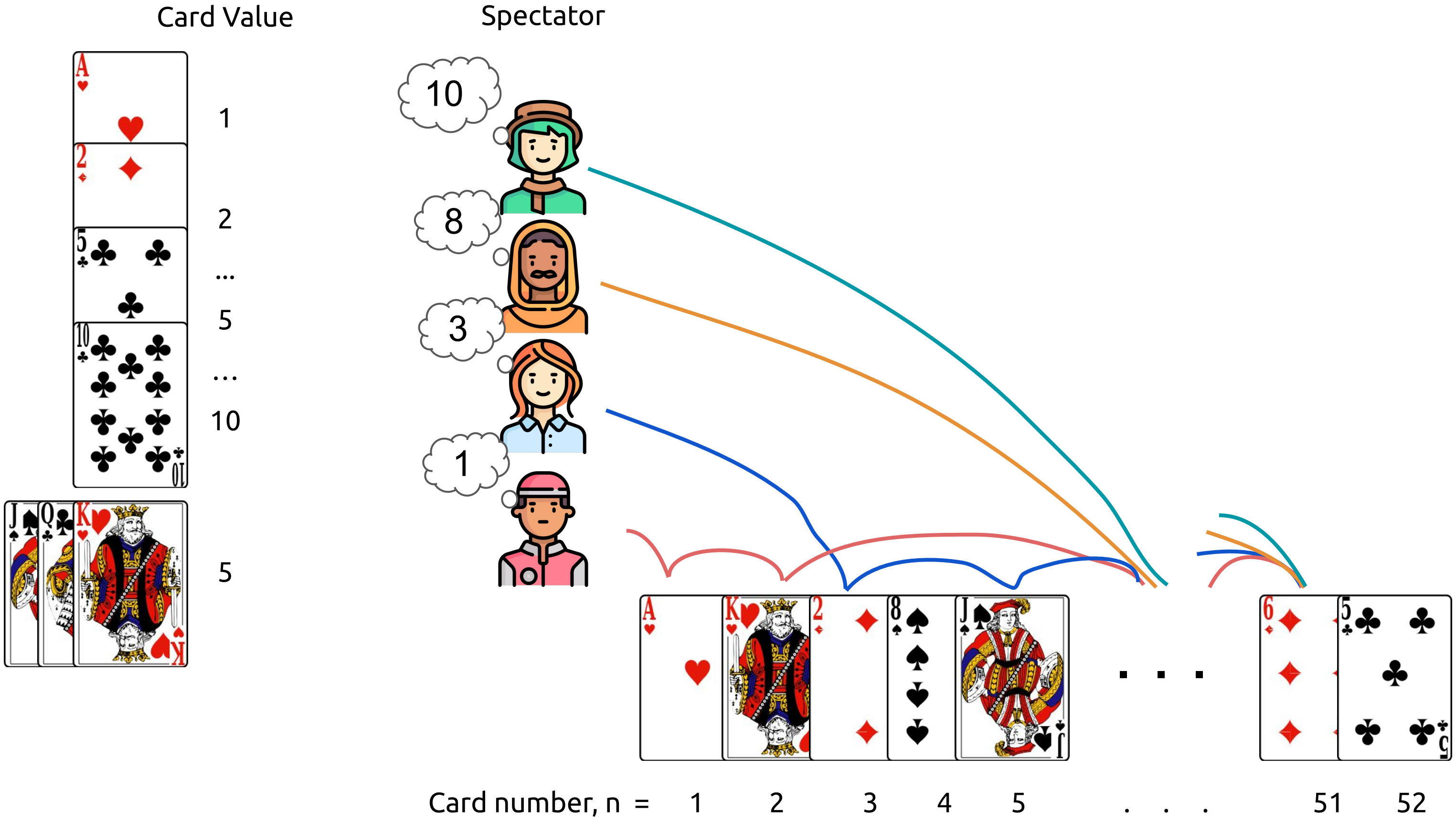
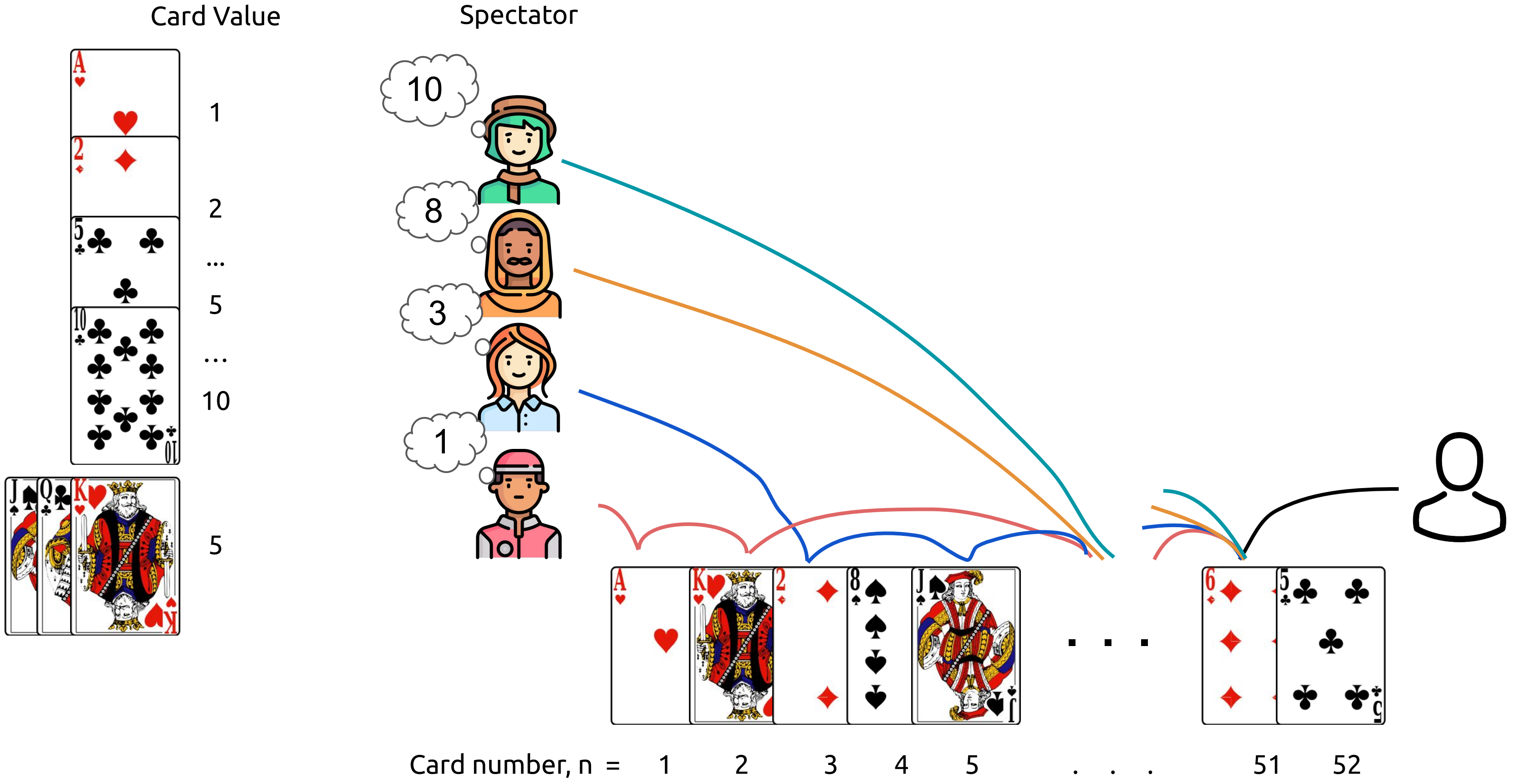


The Law of Large Numbers — Kruskal Count



The Law of Large Numbers — Kruskal Count



The Law of Large Numbers

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The larger the number of cards we use,
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— The End —

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Part 2: The Central Limit Theorem

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Central Limit Theorem

… Coming soon ...